

The impact of resonant magnetic perturbations on runaway electron dynamics

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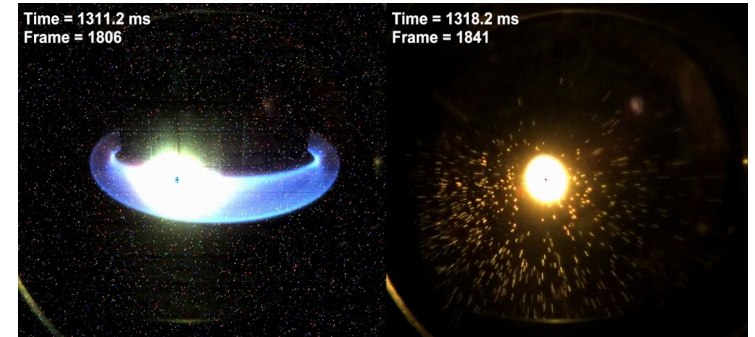


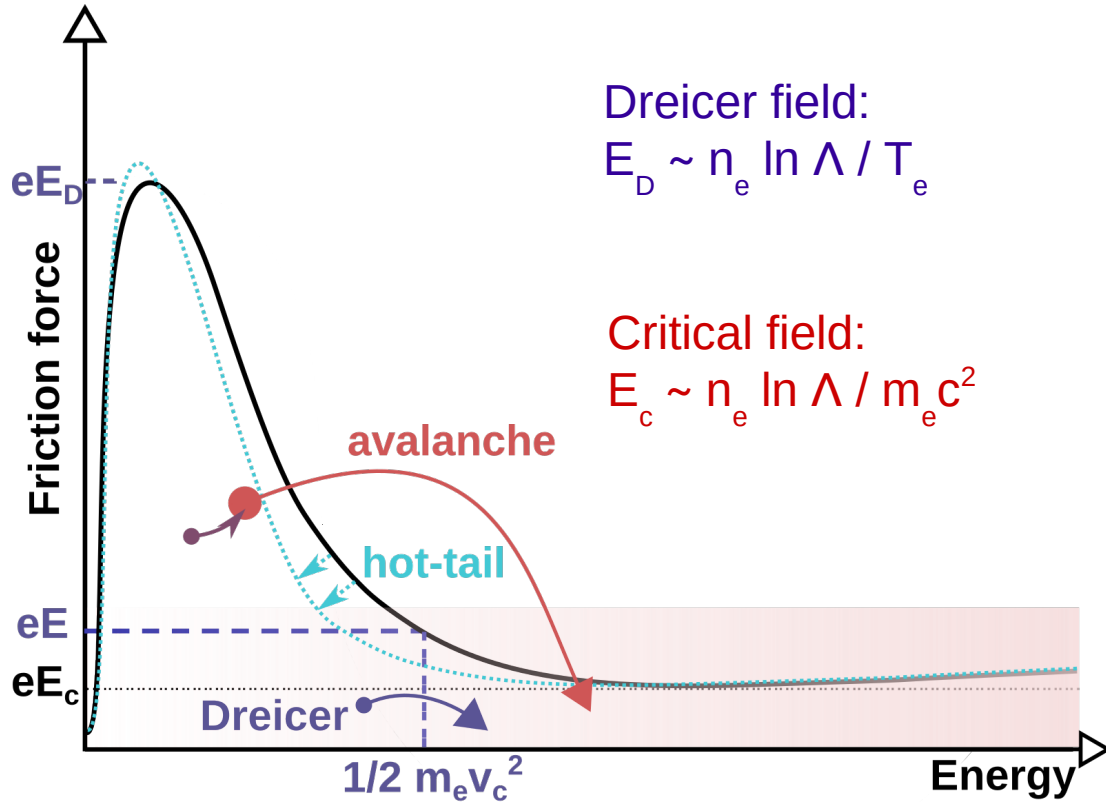
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EUROfusion

- Runaway electrons (RE) and motivation
- RMPs at COMPASS
- RE & RMPs on COMPASS (measurements)
- RE & RMPs on COMPASS (simulations)





Generation mechanisms

Primary: Dreicer

Hot-tail

Compton scattering & Tritium decay

Secondary: **Avalanche**: exponential grow

→ **Disruptions** (TQ – Thermal Quench)

- quick cooling of plasma

→ **CQ** - Current Quench ($\sigma \sim T_e^{3/2}$)

- fast I_p decay → induce **E**

→ **$E/E_c > 1$ in experiments**

- simulations = partial explanation

[Hesslow et al PRL 2017,
Liu et al PRL 2018]

- transport

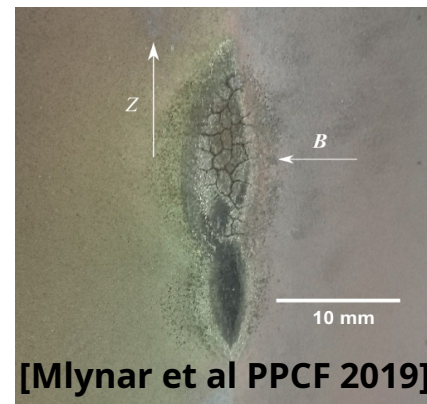
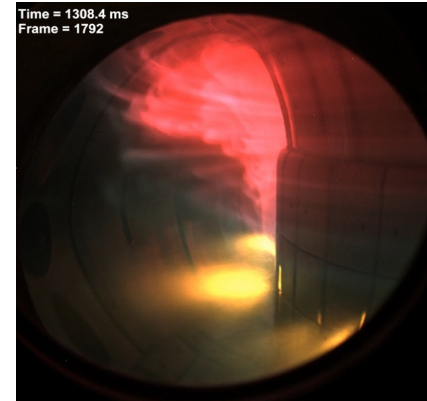
Runaway electrons (RE) [Breizman et al NF 2019]

- relativistic energies
- tokamaks - disruptions, fast Ip decay etc – source of RE
- **serious threat for ITER and other devices**

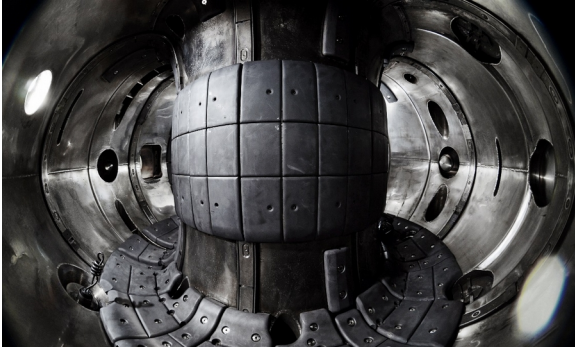
Motivation

- **protection** of current and future devices necessary
- efficient mitigation/prevention **requires deep knowledge** – not possible without **theory and modeling**
- alternative/complementary approaches & feedback
 - **resonant magnetic perturbations (RMPs)** → transport ...
 - **kinetic + MHD instabilities** → pitch angle scattering ...

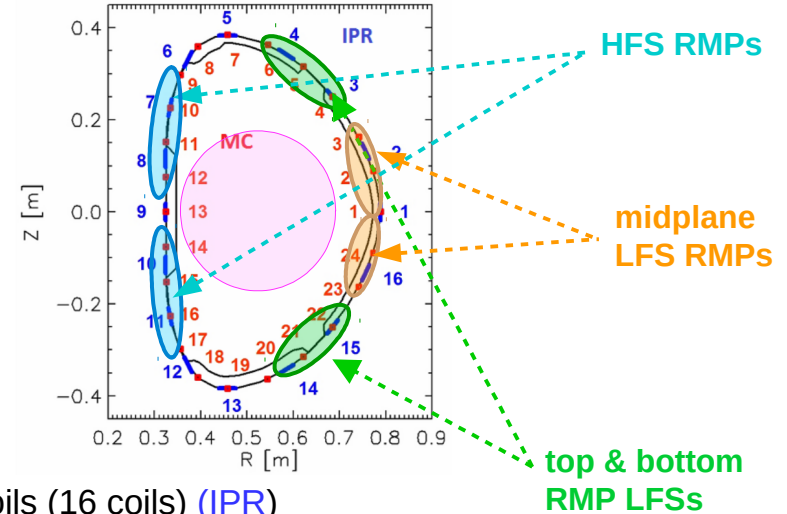
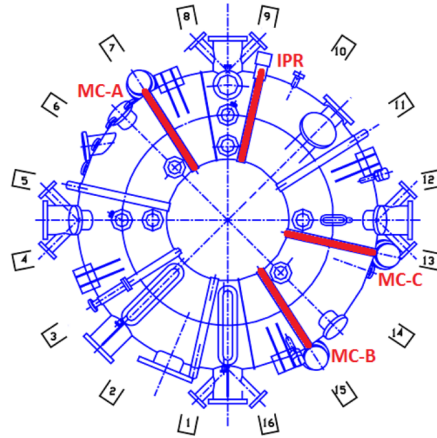
Could RMPs be one/part of the mitigation technique?



COMPASS protruding graphite inner limiter tile



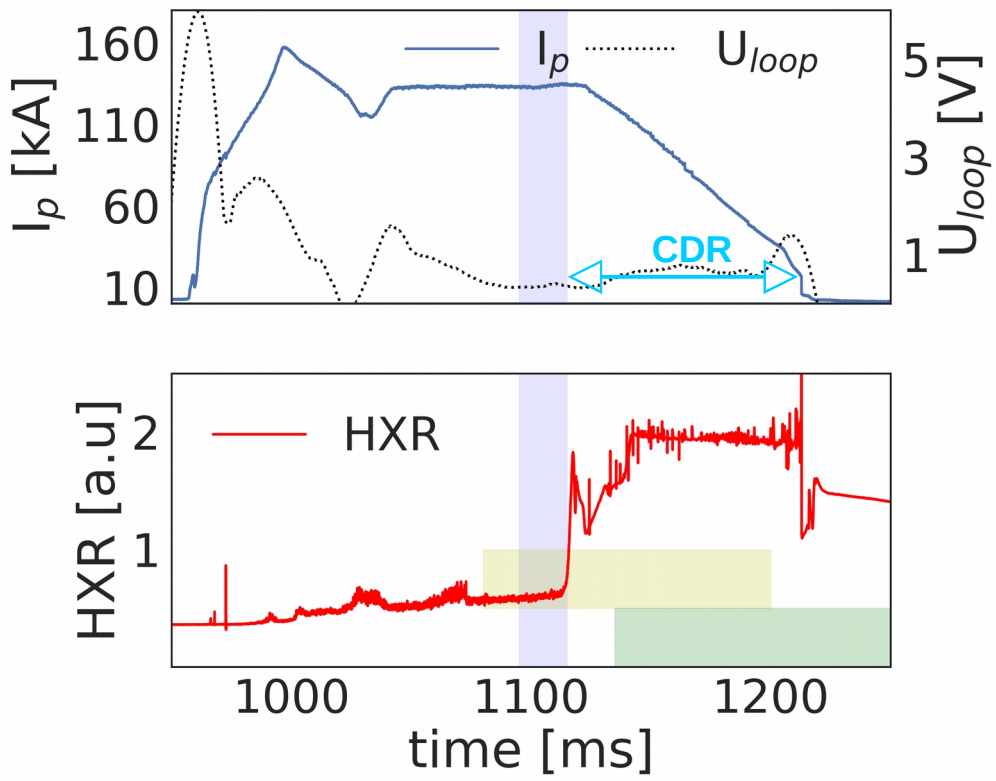
- **ITER-like plasma** $\rightarrow R_0/a = 0.56\text{m}/0.23\text{m}$
- $B_T = 0.9\text{ T} - 1.6\text{ T}$ & $I_p \leq 350\text{ kA}$ & $q_{95} \leq 3$
- MHD, basic and RE diagnostics
- **RMP coils**
 - **HFS**
 - **LFS – off-midplane**
 - **LFS – on-midplane**
 - 4 Power Supplies ($I_{\text{RMP}} \sim 1\text{-}4\text{ kA}$)
 - penetration time $\sim 5\text{ ms}$
 - B_{RMP}/B_T up to 10^{-2}



- Internal Partial Rogowski coils (16 coils) (IPR)
- 3 rings of Mirnov coils (24x3x3 coils each) (MC)
 - \rightarrow radial, toroidal, poloidal magnetic field
- EPR coils + flux loops + saddle coils

RE diagnostics - HXR, photoneutrons, V-ECE, Cherenkov, scintillators, calorimetry head, fast cameras (VIS + IR), SXR, spectroscopy, MediPix, Thomson scattering, interferometer.. [Weinzettl et al. NIST 2017, Havranek et al. FED. 2017]

Reference RE scenario



- reproducible
- gas injection (purple area) = destruction of the thermal plasma
- “zero” U_{loop} [Ficker et al NF 2019]
- **CDR** (Current Decay Rate) = di_{RE}/dt
- **pre-disruption** scenario = RMP applied **before** gas injection (lower RE energy)
- **post-disruption** scenario = RMP applied **after** gas injection (direct impact on RE, low T_e background plasma)

RMPs configurations combined with

- different gas (Ar, Ne, D & their mixtures)
- different types and number of valves

Impact on CDR_{RE} (Current Decay Rate)

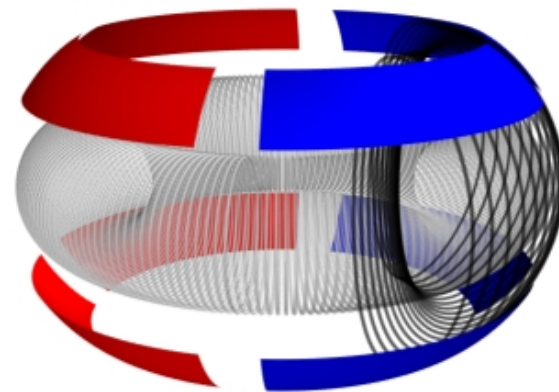
- **the strongest effect (RMP*)** ~ $\frac{3}{4}$ faster CDR
- **the weakest effect** ~ **a few %** faster CDR

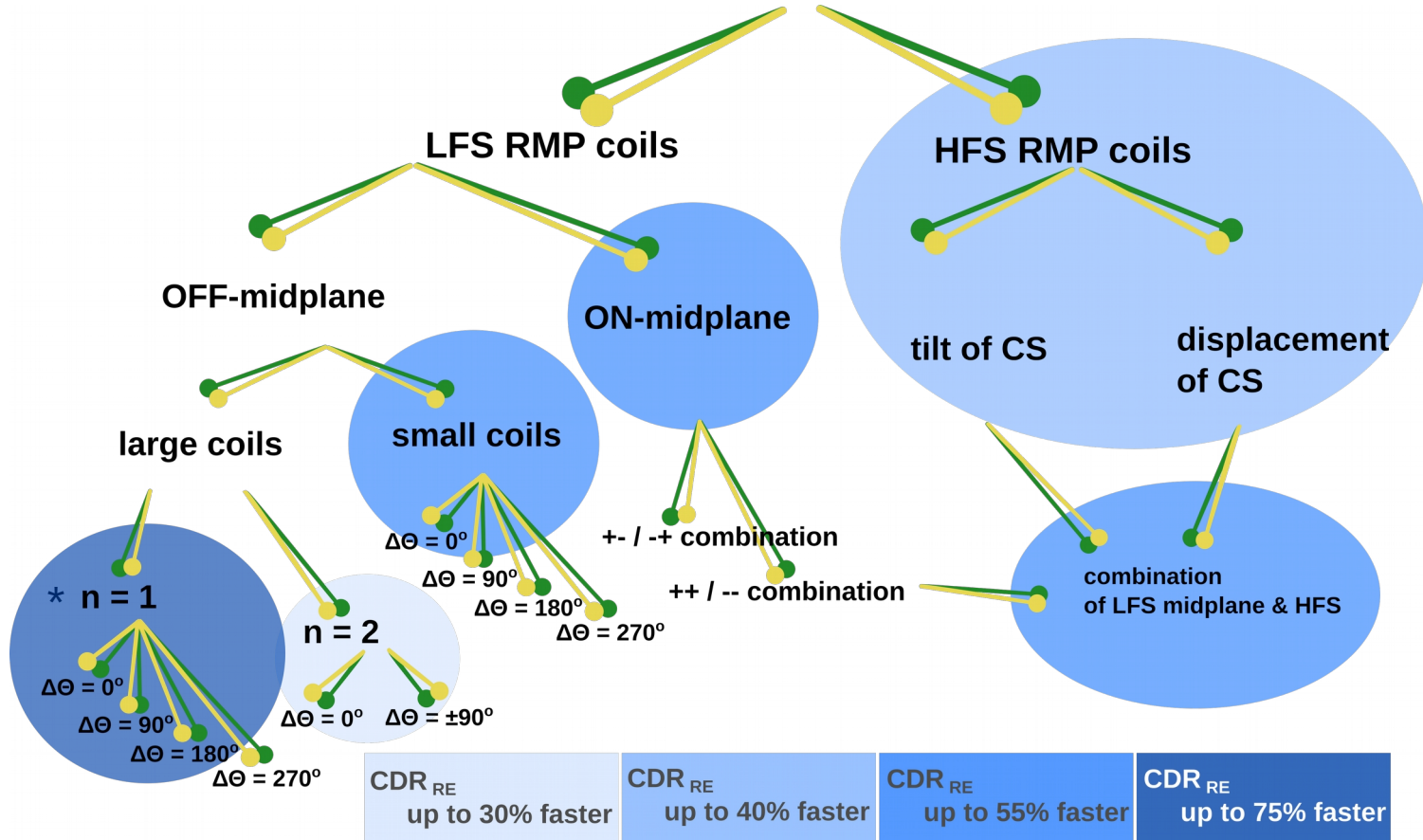
→ the effect **scaled** with

- the size, position, phase and current in RMP coils
- with gas / valve type and amount

→ **RMP* + Ne ~ 20% faster CDR_{RE} than RMP* + Ar**

- other effects – screening, RE energy etc – simulations necessary

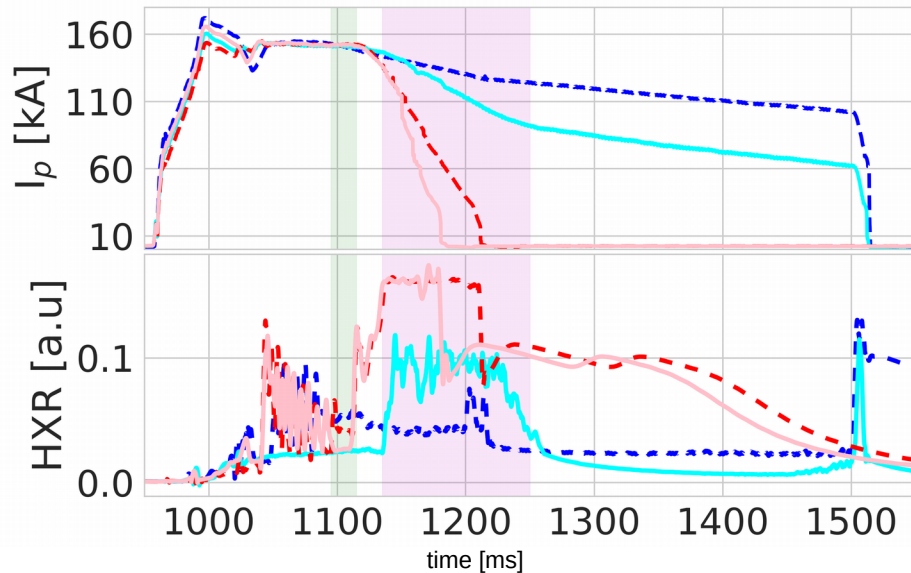




What is affected by RMPs? → amount & energy of RE / RE transport / level of radial fluctuations / plasma response / ...

RMP only / RMP + gas injection

- NO puff & NO RMP (15792)
- puff & NO RMP (15783)
- NO puff & RMP (15786)
- puff & RMP (15784)

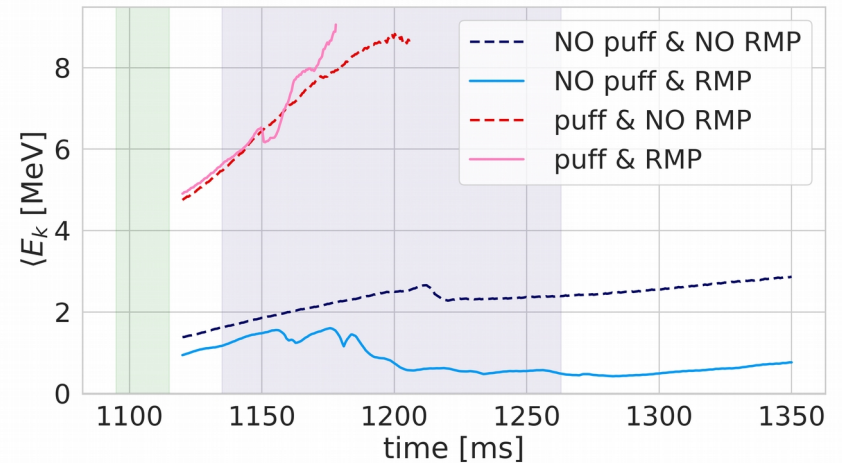


- RE losses already present when RMPs are energized
- HXR signal - saturated (end of the gas injection) ⇒ $n_{RE} > 10^{15}$

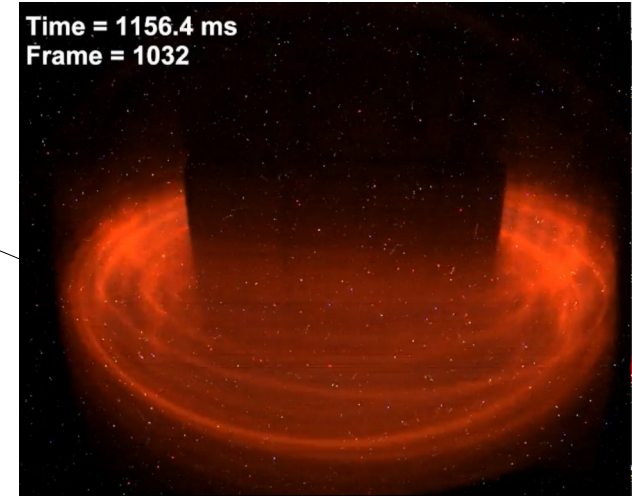
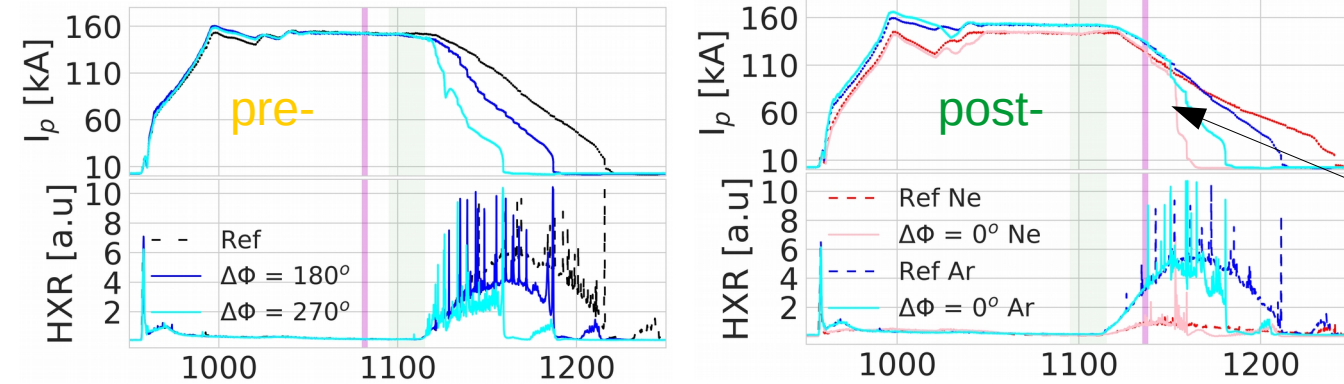
Energy dependence [Ficker et al NF 2019]

$$\langle E_k \rangle \propto R_0 B_v e c$$

E_k → direct dependence on the radial position R_0 and vertical magnetic field B_v



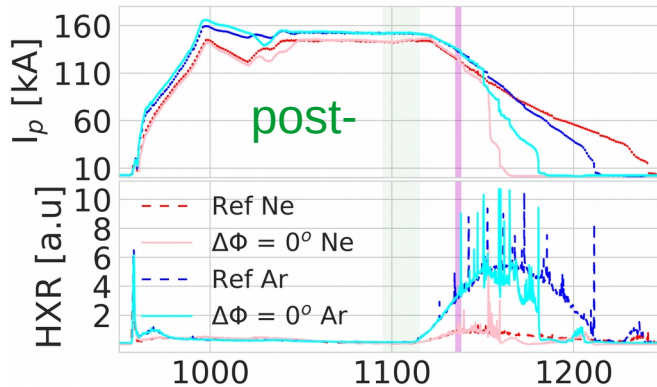
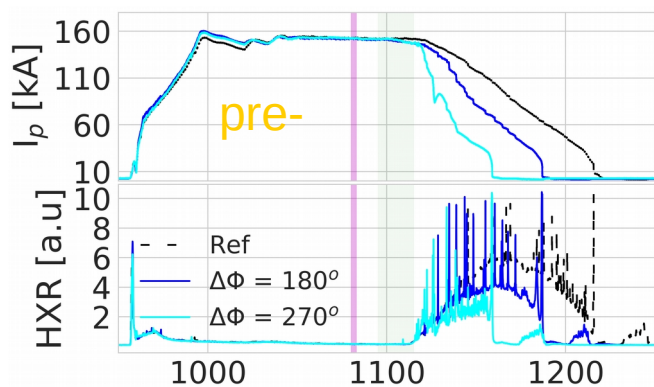
off-midplane LFS RMP ($n = 1$)



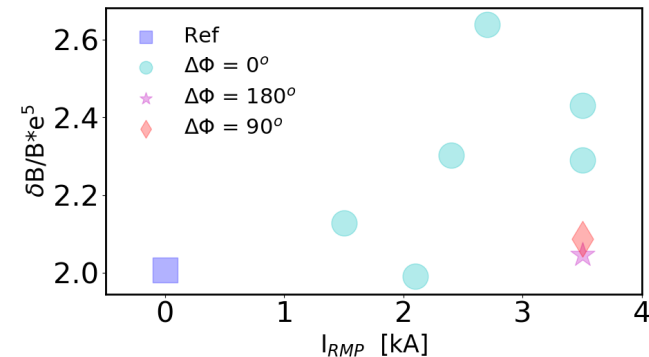
Ar case → for $\Delta\phi=270^\circ$ (pre, max -60%)
 → for $\Delta\phi=0^\circ$ (post, max -45%) scaling with $\Delta\phi, Z_{\text{eff}}, I_{\text{RMP}}$

Ne case → longer RE current ($\sim 40 \text{ ms} > \text{Ar}$)
 → $\Delta\phi=0^\circ$ (post, max -75%) - more scattered effect

off-midplane LFS RMP ($n = 1$)



post-

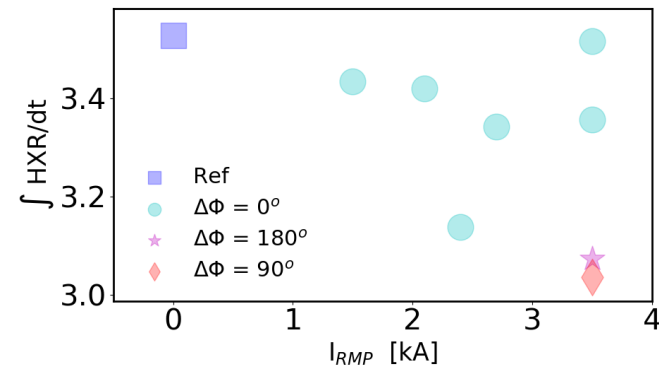


Ar case → for $\Delta\phi=270^\circ$ (pre, max -60%)
 → for $\Delta\phi=0^\circ$ (post, max -45%) scaling with $\Delta\phi, Z_{\text{eff}}, I_{\text{RMP}}$

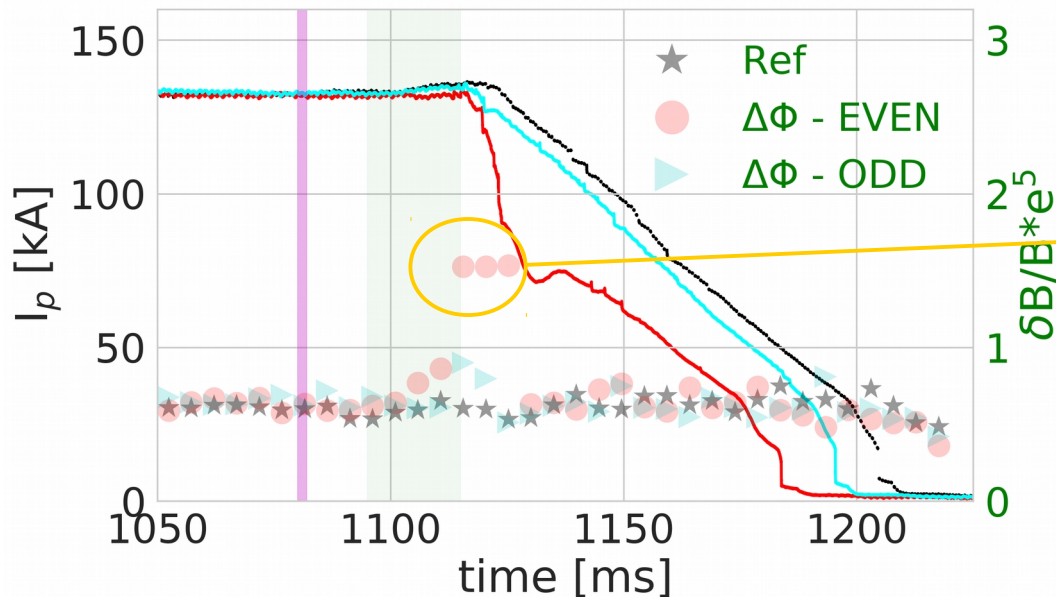
Ne case → longer RE current (~ 40 ms > Ar)
 → $\Delta\phi=0^\circ$ (post, max -75%) - more scattered effect

Radial fluctuations $\delta B_r/B_T$ and $\int \text{HXR}/dt$ scaled with I_{RMP} (post-)

post-

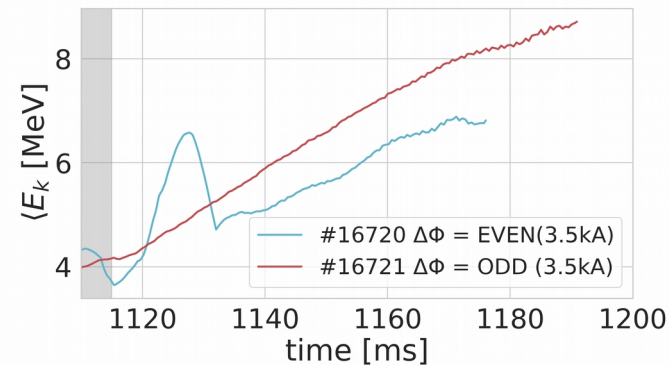
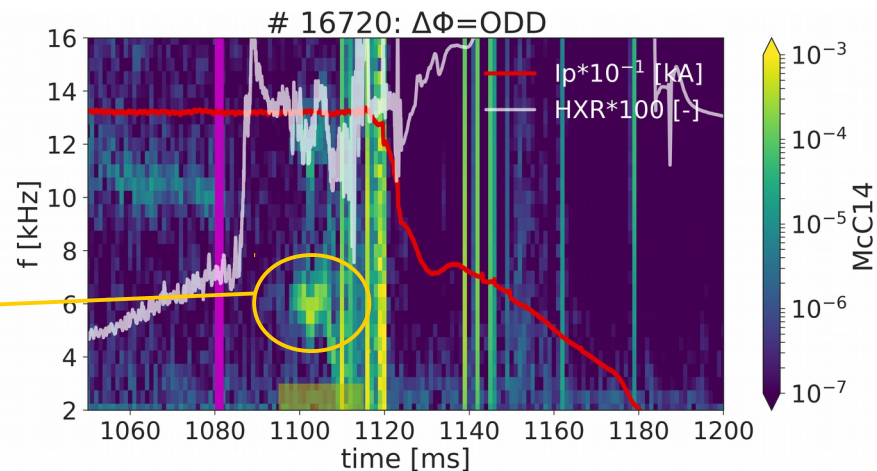


off-midplane LFS RMP ($n = 2$)

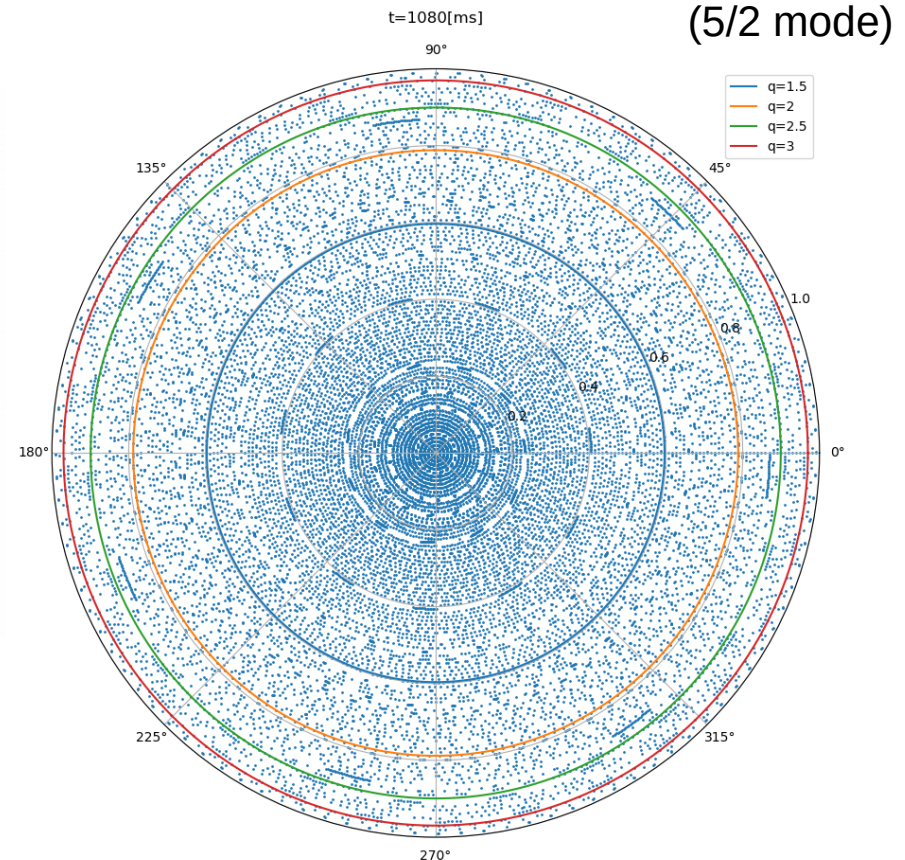
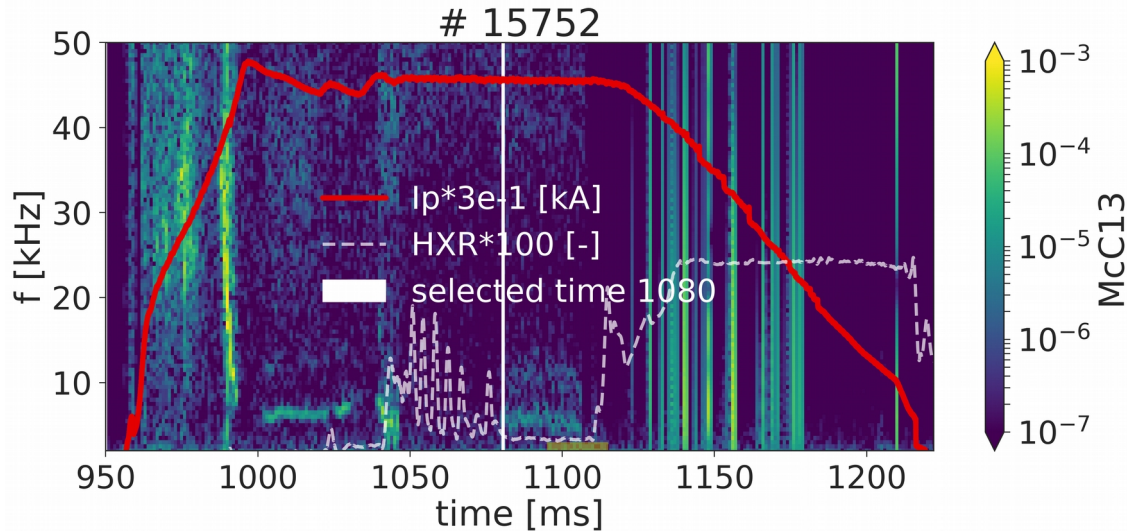


→ MHD activity – rotating island formed ($n=1$) for $\Delta\phi$ – ODD
 - increase of radial fluctuations $\delta B_r/B_T \rightarrow$ drop of I_p & drop of averaged E_k / n_{RE}

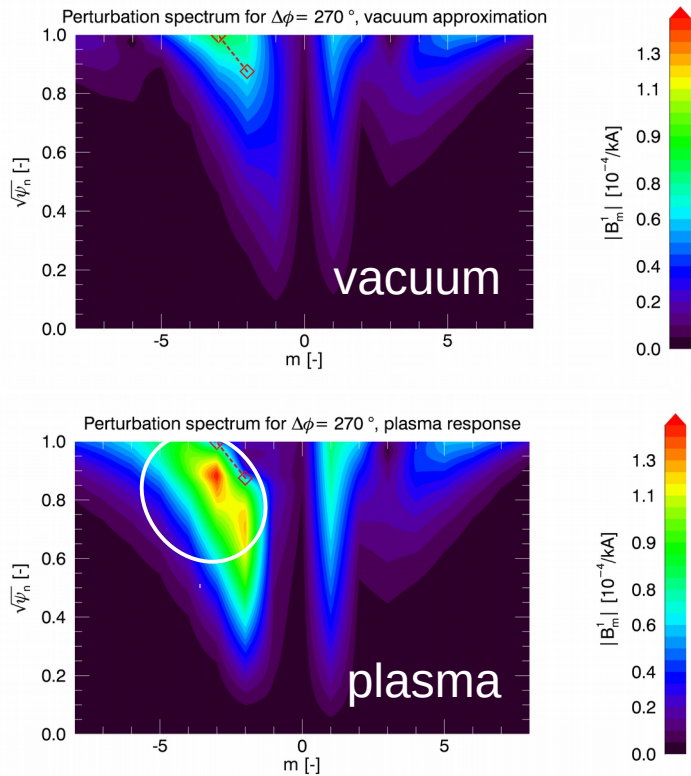
[Gobbin et al EPS 2019, Macusova E et al APS 2018]



Test case - LFS off-midplane RMP ($n = 1$) + Ar



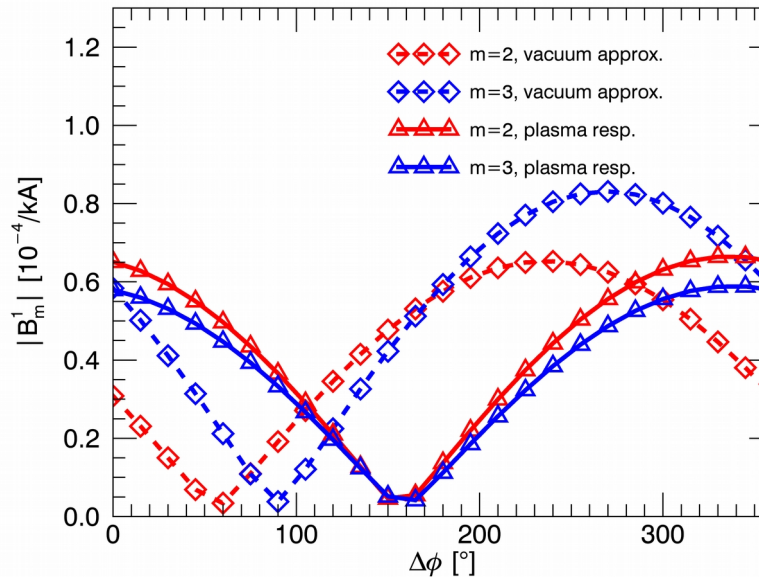
- only weak MHD (5/2) – flux surfaces not influenced
- $t = 1080$ ms (MARS-F & tracing time)
- reconstruction of the magnetic topology
[Casolari et al EPS 2019]



[Mlynar et al PPCF 2019]

MARS-F (n=1)

$\Delta\phi$ dependence of resonance with $q=m/1$ surfaces



- plasma response → m=2 & m=3 maxima shifted to higher $\Delta\phi$ values [300°- 360°]
- similar shift observed at ASDEX [Gobbin et al NF 2018]

MARS-F

[Liu et al PP 2000]
[Liu et al NF 2016, NF 2019]

- resistive MHD code
- one fluid
- toroidal geometry
- curve-linear mag. coord.
- guiding center drift orbit module for RE
- input: T_e, T_i, n_e, v_ϕ profiles
- outputs:
 - eigenvalue solver
 - total field including plasma response

- **RE** - strongly passing (small pitch angle), almost collisionless (high energy RE are immediately lost)
- **RMP or disruption - stochastic** magnetic field at the plasma edge → enhancement of the cross-field transport = increase of losses = can prevent avalanche [**Helander et al PoP 2000**]
→ COMPASS (mainly Dreicer) → RE seed + lower energies

Radial transport - diffusion

[Myra & Catto 1992, Rechester and M. N. Rosenbluth PRL 1978, Izzo et al NF 2011, Abdullaev et al PP 2012...]

→ D_{RE} depends on: collisionality, electric and magnetic field fluctuations

$$D_{RE} = D_{coll} + D_{EF} + D_{MF}$$

$D_{coll} = \langle \Delta x^2 \rangle / \tau_c$ ($\Delta x \sim q / \sqrt{\epsilon} r_L$) → the main effect arises from the Banana-orbit (one order > RE Larmor radius (r_L)) → $10^{-4} - 10^{-5} \text{ m}^2/\text{s}$

D_{EF}, D_{MF} → caused by electrostatic (ES) and magnetic (M) fluctuations - can cause **orbit decorrelation**
→ fluctuations are associated with a potential flow: $v_{E,M} \sim \hat{b} \wedge \nabla \Phi$

- ES & M drifts - caused by EAB, grad-B and curvature
 - their perturbation part do not average to zero over 1 poloidal average = non-zero transport

$$D_E = \pi q R_0 \frac{1}{v_{\parallel}} \left(\frac{\tilde{E}}{B} \right)^2 < D_M = \pi q R_0 v_{\parallel} \left(\frac{\tilde{B}}{B} \right)^2$$

Small-Kubo-number ($K = \tau_c / \tau_{fl}$) regime: τ_{fl} (time of flight for 1 corr. length) $>$ τ_c (corr. time of the perturbation)

- particle do not explore the field structure
- consistent with standard diffusion - D_{RE} analytical formulas [Hauff & Jenko 2009] - scaling with E_{RE}

$$D \sim E^{-1} \text{ w/o FLR correction, } D \sim E^{-2} \text{ with FLR}$$

Large-K regime: → strongly affected by the field structure (can be trapped into coherent structures (magnetic islands) – subdiffusion, analytical formulas rare - [Gruzinov et al 1990]

$$D \sim \lambda^{1.3} V^{0.7} \tau_c^{-0.3}$$

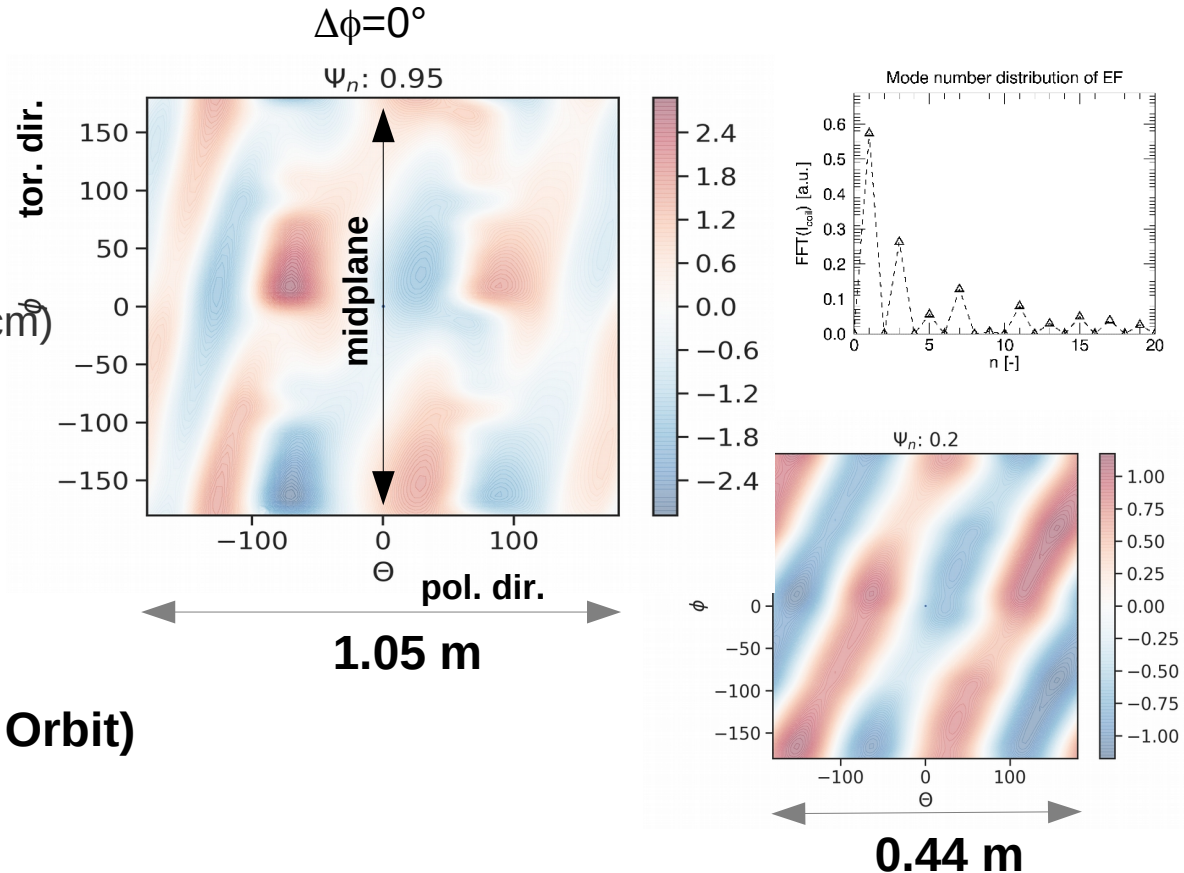
Frozen magnetic field – τ_c replaced by $L_{\parallel} / L_{\perp}$ → $K \sim \delta B / B * L_{\parallel} / L_{\perp}$

REs - expected to be **in orbit-decorrelation regime** and to be trapped in magnetic islands (subdiffusion)

Advection – amplified losses in regions where islands are not present [Sarkimaki et al PPCF 2016]

COMPASS specific characteristic:

- **steep** B-field, E-field, & other **gradients**
- small R_0 = larger toroidal curvature
- r_L comparable with $0.1 \Psi_n$ (at the edge ~ 1 cm) and size of $\delta B/B$ (higher energies)
 - $r_{L-1 \text{ MeV}} > 0.15$ cm
 - $r_{L-5 \text{ MeV}} > 0.7$ cm
 - $r_{L-10 \text{ MeV}} > 1.4$ cm
- RMPs penetrate deep
 - **we need FO (Full Orbit)**



Full Orbit particle tracking code (developed at COMPASS – version 1.0)

modular = each module - different physics or data source

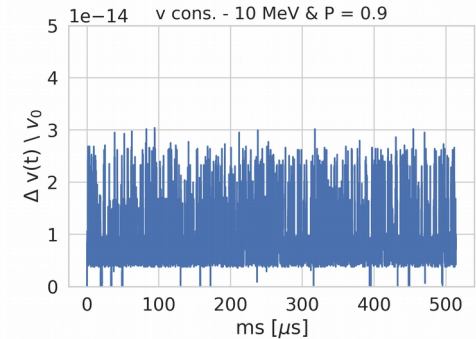
- **3D B-field** – equilibrium & **3D E-field** (toroidal symmetry)
- **3D magnetic perturbation** (MARS-F results) – **no toroidal symmetry**
- particle tracer solves the relativistic equation of motion (1)
- **radiation losses** – LAD force in the Landau – Lifshitz representation
[Landau and Lifshitz 1971, Carbajal et al PP 2017]
- no collisions - for currently used time-scales ($> 1\text{ms}$; $\Delta t = 1\text{e-}13\text{s}$) - future plans
- **r_L averaging** (post processing) – **GC** (future parameter)

$$\frac{d\mathbf{p}}{dt} = -e[\mathbf{E}(\mathbf{x}) + \mathbf{v} \times \mathbf{B}(\mathbf{x})] + \mathbf{F}_R \quad (1)$$

\mathbf{x} and \mathbf{v} - position and velocity of particle

$\mathbf{p} = m_e \gamma \mathbf{v}$ is the relativistic momentum

$\gamma = (1 - v^2/c^2)^{-1/2}$ and \mathbf{F}_R is the radiation reaction force



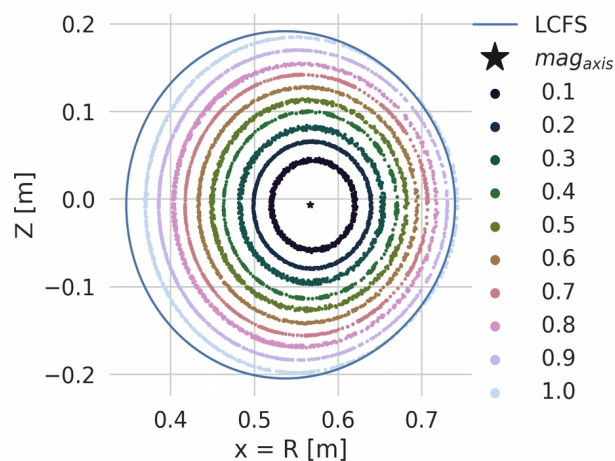
→ validation against experiment

→ first validation against ORBIT* (w/o perturbation) was made ($> 2\text{MeV}$) [Gobbin et al NF 2016]

→ comparison with REORBIT [MARS-F] [Liu et al NF 2019]

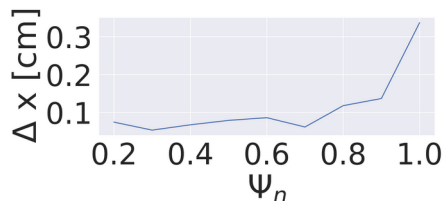
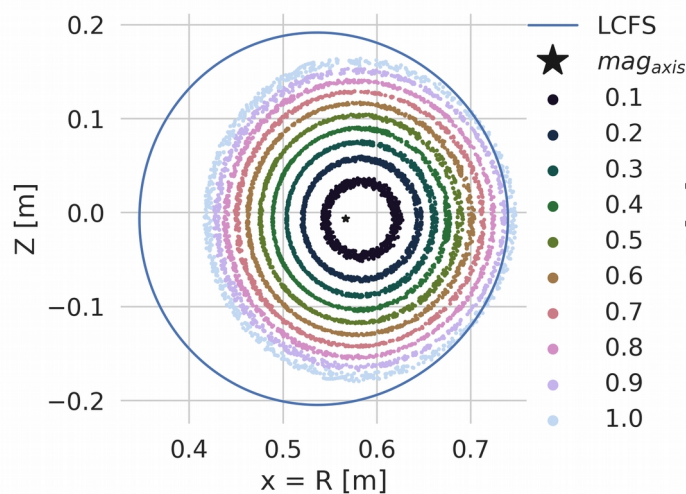
RMP off & E on & F_R on & $\xi = 0.9 \rightarrow$ simulations - 20 μ s (ξ consistent with [Vlainic et al JPP 2015])

1MeV: $r_{L-1 \text{ MeV}} = 0.14\text{-}0.18 \text{ cm}$

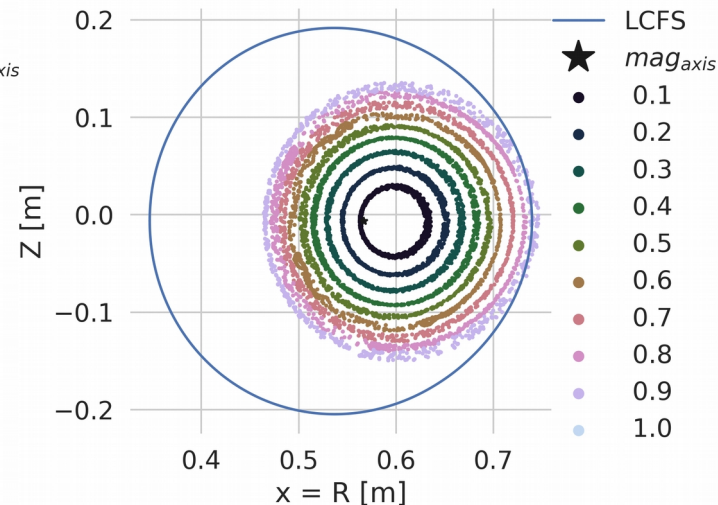


\rightarrow displacement up to 0.1 cm for 1MeV – flat radial profile

5MeV: $r_{L-5 \text{ MeV}} = 0.72\text{-}0.75 \text{ cm}$



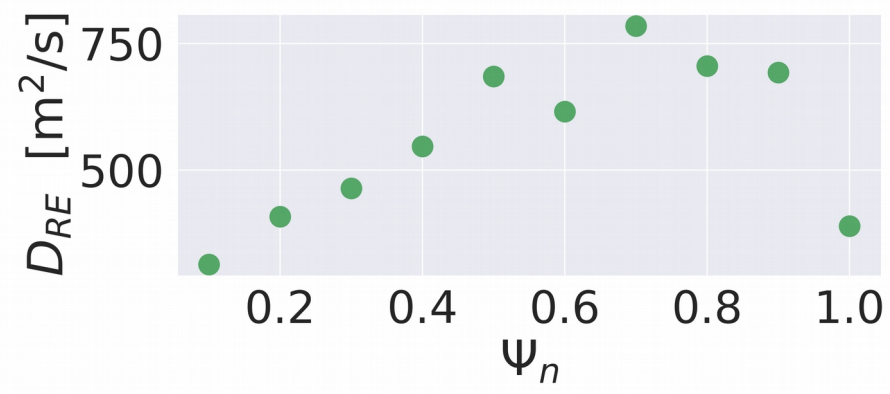
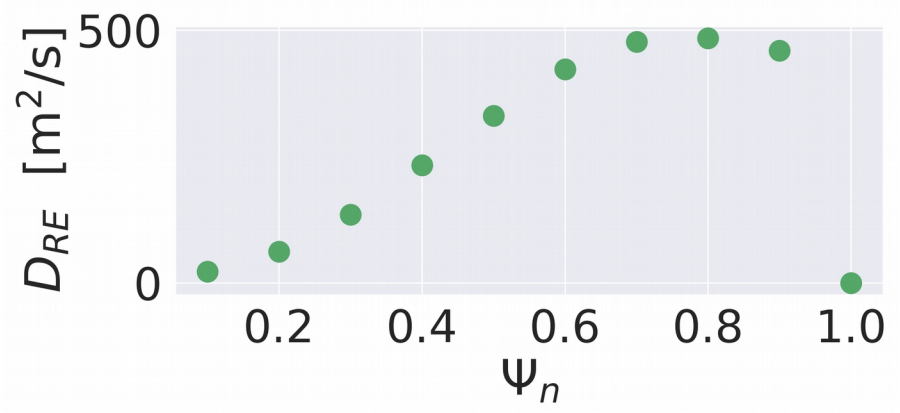
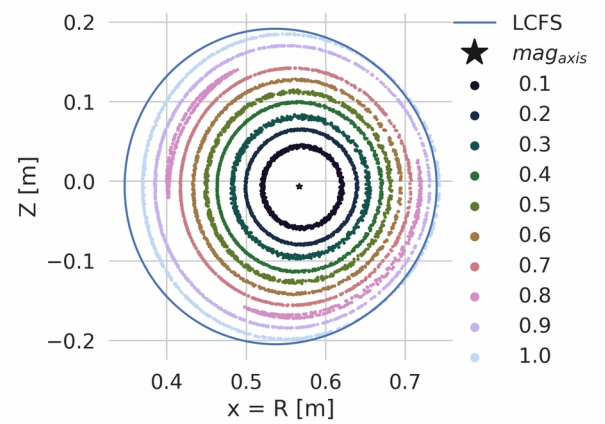
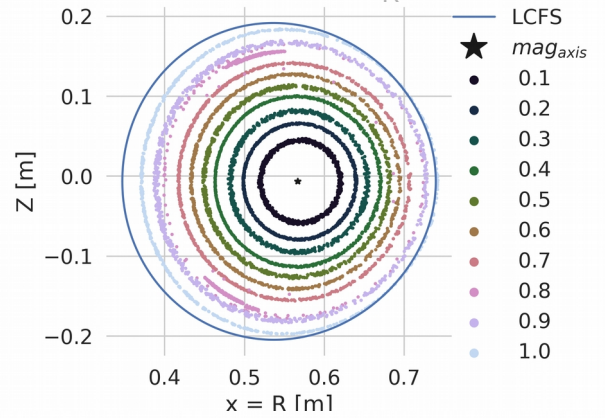
10MeV: $r_{L-10 \text{ MeV}} = 1.45 - 1.6 \text{ cm}$



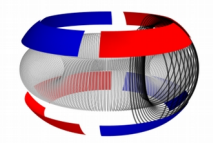
\rightarrow displacement up to 0.2 cm
 \rightarrow time of one poloidal turn $\sim 0.02\mu$ s

similar simulations have been done [Papp et al PPCF 2012]

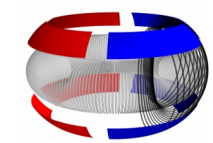
RMP on & E - & F_R - & $\xi = 0.9$



$\Delta\phi = 180^\circ$
 $\delta B/B$ up $1 \cdot 10^{-3}$



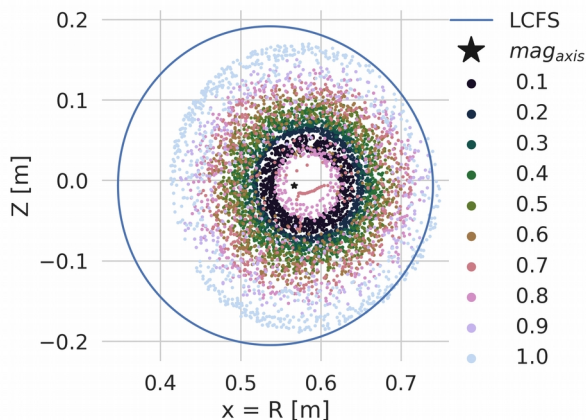
$\Delta\phi = 0^\circ$
 $\delta B/B$ up $1 \cdot 10^{-3}$



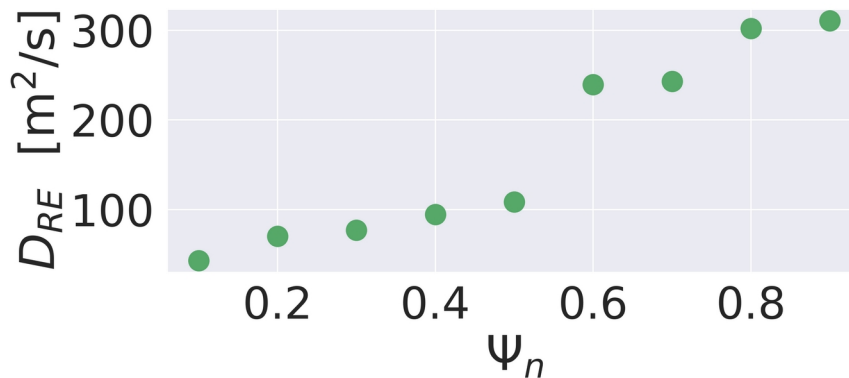
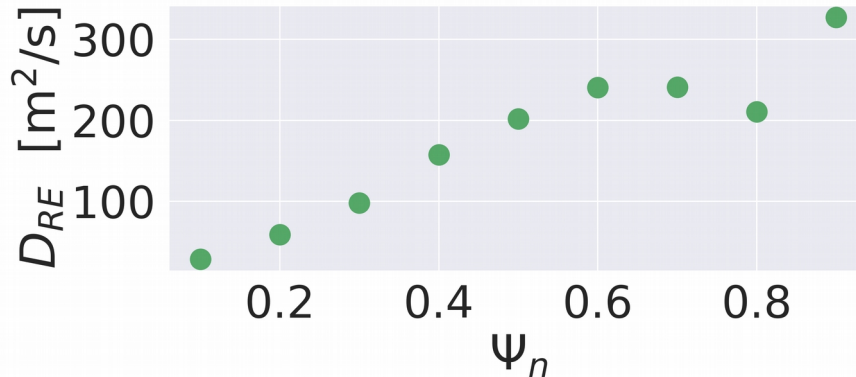
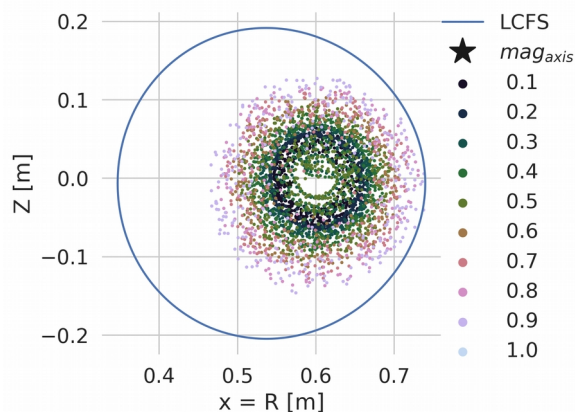
RMP phase shift ($\Delta\phi$)

RMP **on** & E on & FR on & $\xi = 0.9$

5MeV



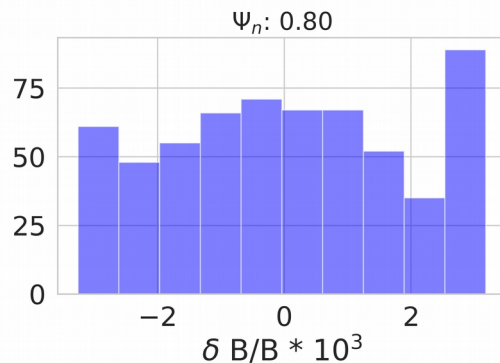
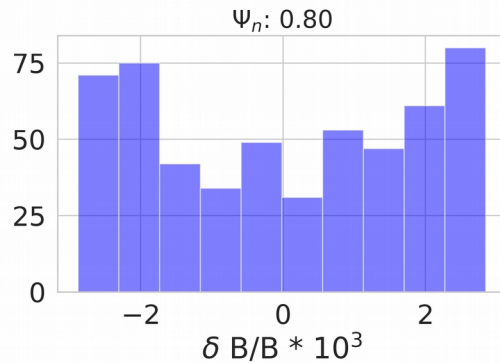
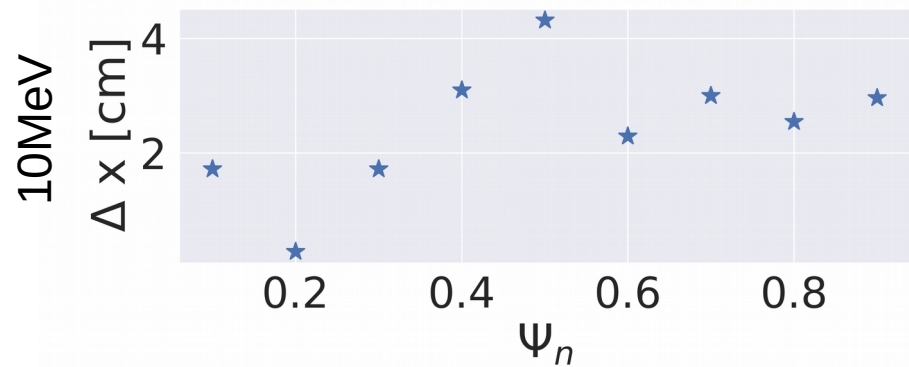
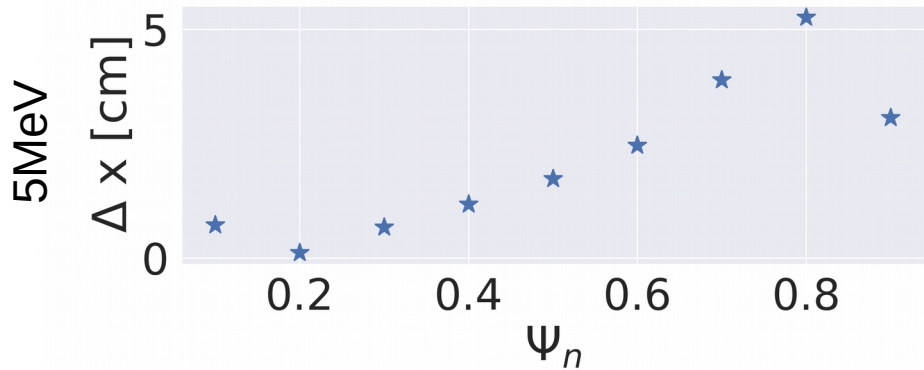
10MeV



$\Delta\phi=0^\circ$
 $\delta B/B$ up $7 \cdot 10^{-3}$

energy
diffusion (partly)

average poloidal displacement



energy ↑
diffusion (partly) ↓

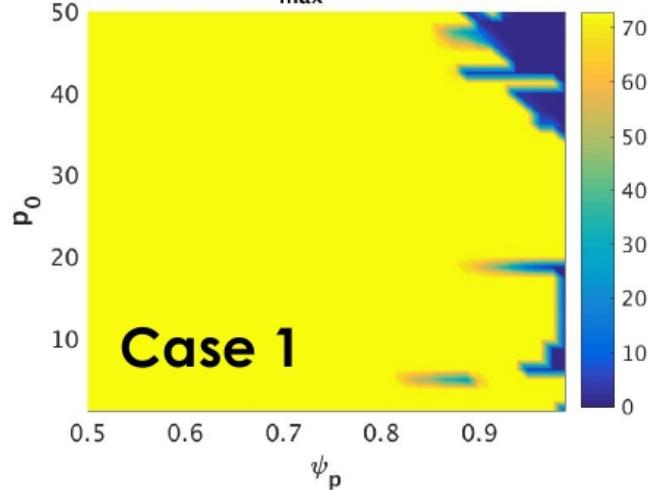
Simulations provided by REORBIT (MARS-F) for n=1 off-midplane LFS RMP [Liu et al. 2019 NF]

- relativistic RE guiding center drift orbit model
- small angle collision with impurity nucleus & SR & Bremsstrahlung drag

I_{RMP} - 2D scan ($\Psi_p \times p_0$) at fixed $\xi = 0.1$ (max. simulation time t_{max} before the particle is lost)

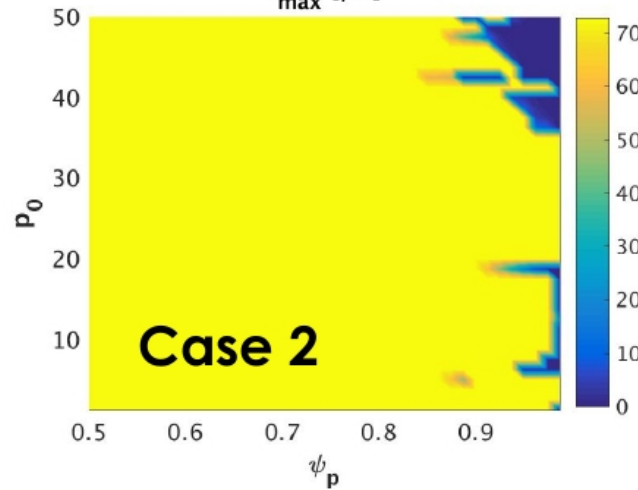
$\Delta\phi = 270^\circ$ ($I_{RMP} = 3.2$ kA)

t_{max} [μs]



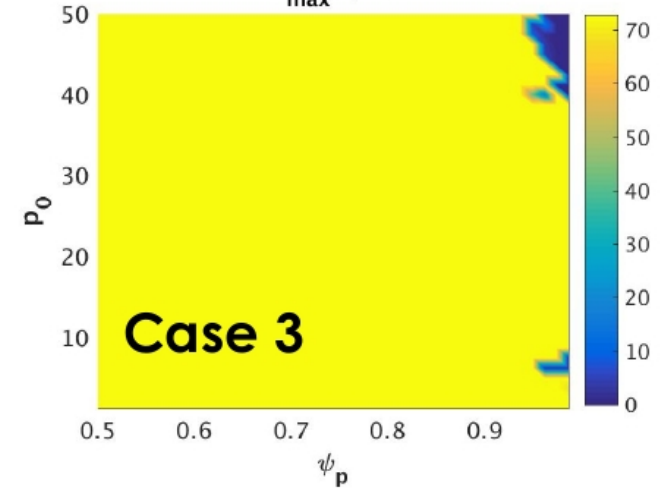
$\Delta\phi = 270^\circ$ ($I_{RMP} = 2.8$ kA)

t_{max} [μs]



$\Delta\phi = 270^\circ$ ($I_{RMP} = 1.2$ kA)

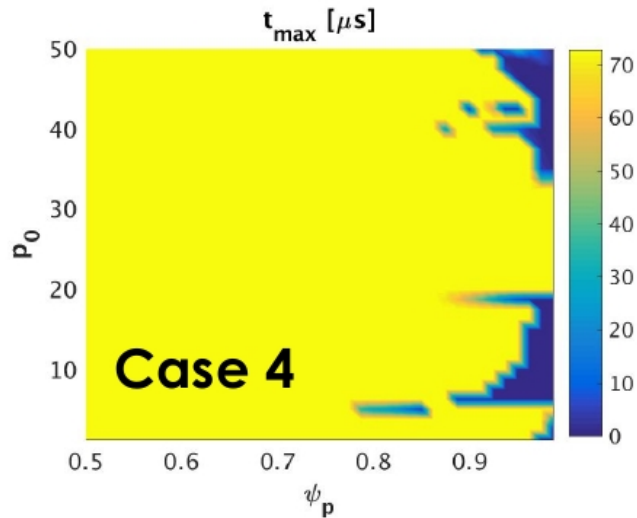
t_{max} [μs]



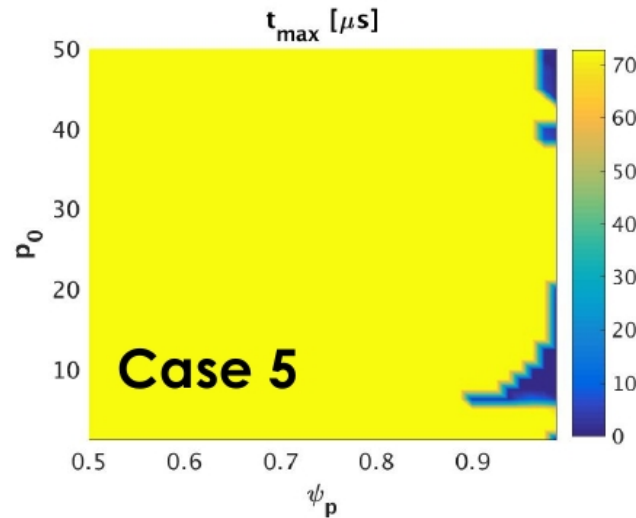
REORBIT (MARS-F) simulations [Liu et al. 2019 NF]

$\Delta\phi$ - 2D scan ($\Psi_p \times p_0$) at fixed $\xi = 0.1$ (max. simulation time t_{\max} before the particle is lost)

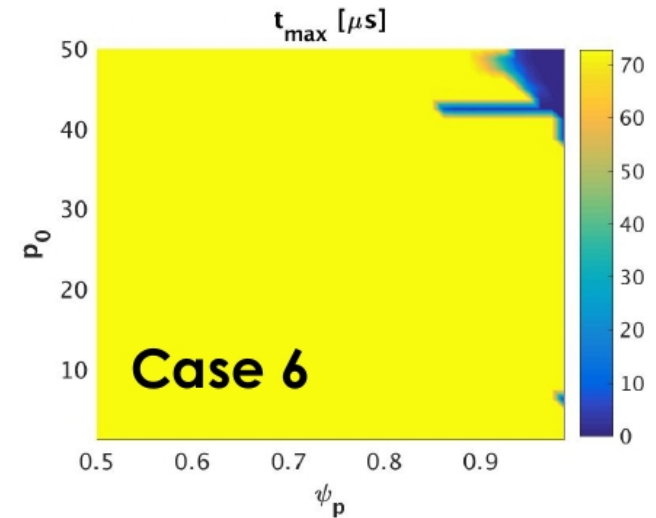
$\Delta\phi=0^\circ$ ($I_{\text{RMP}} = 3.2$ kA)



$\Delta\phi=90^\circ$ ($I_{\text{RMP}} = 3.2$ kA)



$\Delta\phi=180^\circ$ ($I_{\text{RMP}} = 3.2$ kA)



Effect of RMPs at COMPASS

- significant impact on RE population
 - smaller CDR + τ_{RE}
 - **reduction of their energy and amount**
 - smaller final impact of RE on the vessel ($\int HXR/dt$ – smaller)
 - different loss regimes (dependent on I_{RMP}) – excellent for simulations and theoretical predictions testing
- RMP influence the RE trajectories (dependent on the I_{RMP} and phase)
 - **fast losses within 10 μ s were detected**
 - low energetic particles were lost only for the phase when the plasma response was the strongest (preferable energy range < 7 MeV)
 - increase of poloidal orbit displacement (grows with I_{RMP} and $\Delta\phi$, not always with energy)
 - could be a **solution for small compact machines (COMPASS-Upgrade, SPARC etc)**

Plans

- particle simulation of the post-disruption scenarios & other phases & amplitudes & MHD modes
- more modules (collisions / more particles / kinetic solver)