



Recent progress on kinetic-MHD modeling of the interplay between fast particles and macroscopic modes in tokamak plasmas using XTOR-K

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Motivations: fast particles – MHD interaction

- ► ITER: fusion reactions induce fast particles α (3,5MeV) → confinement crucial for energy transfer
- Current tokamaks: fast particles induced by heating sources
 - \rightarrow good proxy to predict α dynamics

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 \succ ITER: fusion reactions induce fast particles α (3,5MeV) \rightarrow confinement crucial for energy transfer Current tokamaks: fast particles induced by heating sources \rightarrow good proxy to predict α dynamics Toroidal > Particles: Direction 3 caracteristic frequencies Separatrix \rightarrow 1/ giration Banana Trajectory \rightarrow 2/ bounce \rightarrow 3/ toroidal precession Projection of Trapped Ion Trajectories is Banana Shaped (for illustration only) X-point lon gyro-motion Divertor Targets

Motivations: fast particles – MHD interaction



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Motivations (2): key issues to be raised in modeling

- Fast particles can destabilize Alfvén Eigenmodes (AE):
 - \rightarrow Alfvén modes stable without fast particles.
 - \rightarrow Fast particles destabilize modes TAE / BAE / RSAE / UKAEA \ldots
 - \rightarrow transport \rightarrow degradation of confinement + losses damaging walls.



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Fast particle interaction with sawteeth:

- \rightarrow Fast particles can either stabilize sawteeth
 - → monster sawteeth [Chapman NF10]
- \rightarrow OR fast particles may destabilize fishbones
 - → combined fishbones/sawteeth [Nave NF91] or no sawteeth [Günter NF99]

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Hybrid kinetic-MHD code XTOR-K

Initially developed by H. Lütjens and J.F. Luciani [Lütjens JCP10]



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Input for the code:

 \rightarrow Equilibrium bulk profiles from CHEASE code [Lütjens CPC96]

- \rightarrow Maxwellian or slowing-down kinetic distribution function
- Boundary conditions: plasma described inside separatrix: OK for core physics

Fishbone/sawtooth dynamics using slowing-down fast-particle distribution [Brochard PhD thesis 2019]

MHD interaction with NBI-induced fast particles

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Linear model for fishbone instability [G. Brochard]

Considers energy principle in kinetic-MHD form:

Kinetic energy of instability $\delta I = \delta W_{MHD} + \delta W_K$

[Chen PRL83, Coppi PFB90, White PFB90, Porcelli POP94] MHD potential energy Fast particle potential energy

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$$\delta W_{K} = -\frac{1}{2} \int d^{3}\mathbf{x} d^{3}\mathbf{v} \boldsymbol{\xi}^{*} \cdot \nabla \cdot (\mathbf{v} \otimes \mathbf{v} \tilde{f}_{h})$$
Perturbed
MHD
displacement
Althoremetric MHD
Althoremetric function

→ Solves complex kinetic-MHD dispersion relation for fishbone instability [Brochard JPCS 2018]

 \rightarrow Thin orbit width $\rightarrow \beta_{fast} << \beta_{total}$

Model hypotheses:

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Linear model for fishbone instability [G. Brochard]



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$$\overset{\text{Perturbed}}{\overset{\text{MHD}}{\text{fast particle}}}$$

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[Brochard JPCS 2018]

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Model hypotheses:

 $\rightarrow \beta_{\text{fast}} << \beta_{\text{total}}$

Goal: quick linear stability analyses for internal kink and fishbone \rightarrow pave the way for long non-linear simulations with XTOR-K

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2 branches of instabilities on q=1 depending on fast particle fraction: kink or fishbone modes

- Circular ITER-like test case :
 - → Isotropic slowing-down distrib., peak energy of 1MeV
 - \rightarrow peaked fast particle density:

 $n_{\alpha}(r) = n_{\alpha,0}(1 - r^2)^6$



2 branches of instabilities on q=1 depending on fast particle fraction: kink or fishbone modes

Circular ITER-like test case :



>

Resonant regions in phase-space

> Passing VS trapped particles characterized by pitch-angle $\lambda \propto \mu$ → here trapped: $\lambda > 0.87$



Zones of precessionnal resonance similar in linear model and XTOR-K

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> MHD interaction with NBI-induced fast particles

ITER 15MA scenario: fishbone may be unstable below expected fast particle fraction

- Realistic ITER 15MA scenario
 - $\rightarrow n_{i0} = 10^{20} m^{-3}$ $\rightarrow T_{i0} = T_{e0} = 23 \text{ keV}$ Profiles as in integrated modeling codes
 - \rightarrow slowing-down distrib of α (birth @ 3,5MeV) \rightarrow Goal \blacksquare : check fishbone stability in ITER + study dynamics



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- For $q_0 = 0.95 0.9$, threshold for fishbone instability: $p_{fast} / p_{tot} = 6-10\%$
- ► ITER physics basis $p_{fast} / p_{tot} > 15\%$ → fishbone-unstable!







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Chirping during fishbone oscillations...





associated with flattening of resonant fast particle profile





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MHD interaction with NBI-induced fast particles
 New features in XTOR-K: collisions and NBI
 Ongoing work towards fishbone induced by NBI

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MHD interaction with NBI-induced fast particles → New features in XTOR-K: collisions and NBI → Ongoing work towards fishbone induced by NBI

Feat #1: Collisions in XTOR-K [Timothée Nicolas]

XTOR-K contains kinetic markers and fluid populations



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Domain decomposition needed for collisions



speed-up = 1.7 times

Feat #2: Realistic fast ion source induced by Neutral Beam Injection (NBI) [F. Orain]

- → Kinetic module: neutral particle source reproduce experimental geometry
- → Injection rate depends on beam power and energy
- → Neutral particles follow a line towards a target point with random deviation



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- → Kinetic module: neutral particle source reproduce experimental geometry
- → Injection rate depends on beam power and energy
- → Neutral particles follow a line towards a target point with random deviation
- → Along this line, cumulative ionization probability is calculated :



$$1 - P(l) = (1 - P(l - \Delta l)) \exp(-n_e \sigma \Delta l)$$

with ionization cross-section $\sigma = f(n_e, T_e, Energy) \rightarrow$ fit takes into account atomic physics [Suzuki PPCF98] \rightarrow When 1 - P(l) < random threshold: particle is ionized.

NBI-induced fast ion source validated for AUG case

→ Experimental geometry and equilibrium profiles from AUG shot #23076 [Acknowledgement to Giovani Tardini, IPP Garching]

 \rightarrow Experimental NBI source geometry: radial and tangential sources



(a.u.)

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- \rightarrow New features in XTOR-K: collisions and NBI
- \rightarrow Ongoing work towards fishbone induced by NBI

Initial condition: equilibrium bulk plasma : 99% fluid (MHD) + 1% kinetic (maxwellian)

> 2 steps:

1/ NBI ON + collisions ON. Constant MHD fields2/ NBI OFF, MHD evolution ON, collisions still ON.

ITER-like 15MA simulation with 1NBI: step#1

- 1st step: NBI ON + collisions ON. Constant MHD fields
 - \rightarrow 1 NBI tangential source, P_{NBI}=16.5 MW, E_{particle}=1MeV
 - \rightarrow Increased collision rate and P_{NBI} x10³-10⁴ to reduce computation time





Initial 1% bulk=kinetic







Step#2: Case #1: reduced E_{NBI} and bulk density: no effect of NBI on kink/fishbone stabiliity

- > 2nd step: NBI OFF, MHD evolution ON, collisions still ON.
 - \rightarrow self-consistent interaction between MHD and NBI-injected fast particles
 - \rightarrow Goal \blacksquare : check if NBI can induce fishbone in ITER

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- 2nd step: NBI OFF, MHD evolution ON, collisions still ON.
 → self-consistent interaction between MHD and NBI-injected fast particles
 → Goal (: check if NBI can induce fishbone in ITER)
- ▶ Test case #1: E=1MeV → E=100keV ; $n_e = 1 \times 10^{20} \text{m}^{-3} \rightarrow n_e = 3 \times 10^{19} \text{m}^{-3}$



Step#2: Case #2: realistic E_{NBI} and bulk density: still no fishbone-resonant configuration

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- \blacktriangleright Test case #2: E=1MeV ; n_e=1x10²⁰m⁻³ $F(E,\lambda)$ trapped 1.15 300 1.1 250 Ē 1.05 200 μB_0 1 150 $\overset{\parallel}{\sim}$ 0.95 100 0.9 50 0.85 0 0.2 0.4 0.6 0.8 0 E (MeV) Very few particles in fishbone-resonant zone: still internal kink

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Very few particles in fishbone-resonant zone: still internal kink

E (MeV)

Additional work in progress: extend computational domain, including SOL, coils and wall

Enabling Research project "kinetic MHD and control opportunities":
 PI Timothée Nicolas

- \rightarrow Domain extension validated in vacuum [A. Marx PPCF2017]
 - \rightarrow Under development for plasma with resistive wall
 - \rightarrow First external kink modeling ongoing



Conclusion

XTOR-K : hybrid MHD + kinetic

→ new features: linear fishbone model for predictions, collisions, NBI
 + ongoing: extend computational domain to SOL and wall

 \rightarrow allows to model realistic tokamak physics in the core + soon at the edge

➤ Linear model + XTOR-K with slowing-down fast particle distrib: → ITER: Fishbone unstable below expected $β_{fast}$ threshold → chirping of fishbone with resonant transport

> XTOR-K with NBI and collisions:

- \rightarrow Realistic fast particle distribution relaxes towards slowing-down
- \rightarrow ITER: on the way to check if NBI can induce fishbone

THIN ORBIT WIDHT ASSUMPTION INCORRECT FOR E_b > 1MeV



At high energies, the linear model thin orbit width approximation breaks down

Linear verification cannot be performed for E_b > 1 MeV

LOW EP PRESSURE APPROXIMATION NOT VALID AT E_b < 1MeV



> For low **birth energy** (< 1MeV), **fishbones triggered** with $p_h \sim p_{tot}$

> EP pdf with $E_b < 1$ MeV not suitable for linear verification

WEAK OVERALL TRANPORT IN ITER



> Overall EP transport in core plasma around 6% in the fishbone phase

Effects of the alpha fishbone instability on fusion performances limited

Fast mode chirping may prevent to transport large amount of EP

 $\mathrm{d}f$ f $\mathrm{d}t$

 $m_{\rm h}$

Ζ

 \mathbf{E}

Φ

y

 \vec{u}

 \dot{v}_b

Х

Binary collisions

$$\mathcal{C}[f,f] = \frac{(Ze)^{4} \mathbf{\Lambda}}{8\pi\varepsilon_{0}^{2}m} \frac{\partial}{\partial \boldsymbol{v}} \cdot \int \bar{U}(\boldsymbol{v}-\boldsymbol{v}') \cdot \left(\frac{f(\boldsymbol{v}')}{m} \frac{\partial f(\boldsymbol{v})}{\partial \boldsymbol{v}} - \frac{f(\boldsymbol{v})}{m} \frac{\partial f(\boldsymbol{v}')}{\partial \boldsymbol{v}'}\right) \mathrm{d}^{3}\boldsymbol{v}'$$

$$\mathbf{\Lambda} = \log\left(\frac{b_{\max}}{b_{\min}}\right) \qquad \mathcal{C}[f,f] = -\frac{\partial}{\partial \boldsymbol{v}} \cdot \left(\mathbf{F}f - \frac{1}{2}\frac{\partial}{\partial \boldsymbol{v}} \cdot \left(\bar{\mathbf{D}}f\right)\right)$$

$$\bar{\mathbf{v}}_{a} \underbrace{\mathbf{v}_{a}}_{\bar{\mathbf{v}}_{a}} \underbrace{\mathbf{v}_{a}}_{\bar{\mathbf{v}}_{b}} \qquad \mathbf{F} = \frac{\langle \delta \boldsymbol{v} \rangle}{\delta t} \qquad \bar{\mathbf{D}} = \frac{\langle \delta \boldsymbol{v} \delta \boldsymbol{v} \rangle}{\delta t}$$

- Select the two angles so that on average, friction and dissipation have their theoretical values
- Calculation is O(N)
- **Equivalent to Landau-Fokker-Planck [Bobylev PRE 2000]**

Binary collisions are NOT Rutherford collisions!!

Improvement of code execution thanks to domain decomposition, even including collisions

Domain cloning	Domain decomposition
Move: ~30s	Move: ~11.5s
Deposition: <1.5s	Deposition: >1.5s
Nonlinear solver: ~3s	Nonlinear solver: ~3s
Total: ~36s/time step	Collisions: <0.1s
	Total: ~21s/time step

- □ The acceleration is only due to
 - Avoided cache miss
 - Change of field advance (done inside the loop to avoid one dcopy per particle step)
- No optimization to adapt to domain decomposition of
 - Particle deposition
 - MPI reduce

Inter- and intra-species collisions



□ Inter-species binary collisions

- Energy conservation is only statistically guaranteed, because of weight difference [Nanbu JCP 1998]
- Conservation is exact in the case of intra-species collisions



□ Langevin collisions on the electrons

Electrons are assumed at rest (otherwise incompatibility with artificially high resistivity)

Neoclassical tests difficult

A priori the code contains ion neoclassical physics, in particular if the main ion is mainly kinetic. However with a full-f description, PIC noise is very large on velocity.

$$\frac{\Delta V}{V} = \frac{1}{\sqrt{N}} \frac{\sqrt{\langle \overline{x}^2 \rangle}}{\langle x \rangle} \qquad \qquad \frac{\Delta T}{T} \simeq \frac{\sqrt{2}}{\sqrt{N}}$$

Velocity PIC noise is amplified, compared to temperature, by a large factor:

$$\frac{v_{th}}{v} \sim v_{i}^{\star} \frac{L_T}{\rho} \propto T^{-1/2}$$

For the moment, not enough numerical ressources to test the full neoclassical transport. Research ongoing.